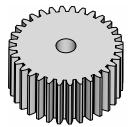
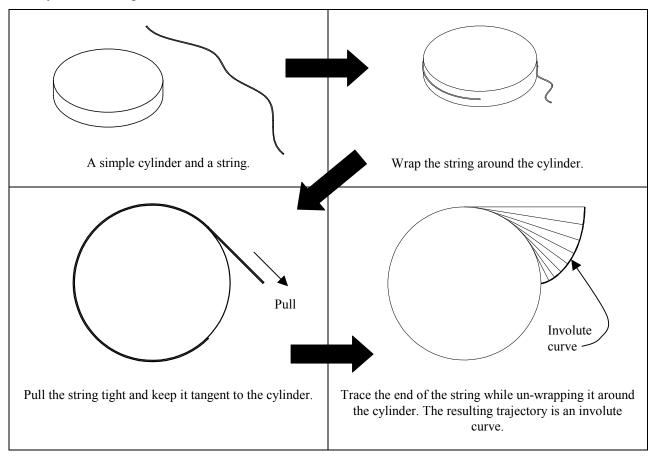
Involute Gears



Introduction

This lesson covers the development of 'involute' gears. An involute gear is based on an involute curve, which is a mathematical shape. To understand what an involute is, consider a simple cylinder and a string as shown below. Wrap the string around the cylinder. While maintaining tension on the string, trace the path that the end of the string makes while un-wrapping it around the cylinder. This path is an involute curve.



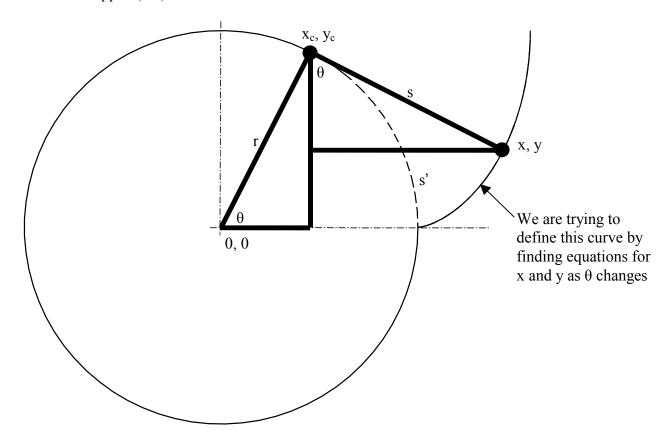
There are two key parameters that control the involute curve: the diameter of the cylinder and the angle that the string is un-wrapped around the cylinder. In the example above, the string is unwrapped 90° around the cylinder.

The Involute Curve

Development of the mathematical equations for the involute curve uses simple trigonometry. We will develop the equations for 90° of one full involute. In other words, we are un-wrapping the string 90° around the cylinder in a counterclockwise direction.

The circumference of a circle is defined by: $c = 2 * \pi * r$ One quarter (90°) of the circumference of a circle is then: $c = \pi * r / 2$

In the figure below, the line 's' is the same length as the part of the circumference the string has been un-wrapped (s').



Using trigonometry, we find that:

$$x_c = r * \cos \theta$$
 $x = x_c + (s * \sin \theta)$
 $y_c = r * \sin \theta$ $y = y_c - (s * \cos \theta)$

Datum Curves From Equation

In Pro/ENGINEER, datum curves can be defined using mathematical equations. When using this feature, a system variable 't' is used, that varies from 0 to 1 over the length of the curve. For the involute curve, let the angle (ang) be equal to 't' times 90. This means that the variable 'ang' will vary from zero to 90°.

To define 's', we combine the circumference equation and 't' to form:

$$s = (\pi * r / 2) * t$$

In this example, the diameter of the cylinder is 1.500. This is the *base diameter* in gear design terminology. The radius (r) of the cylinder is 0.75 inches.

The equations for Pro/ENGINEER are:

$$r = 0.75$$

$$ang = t * 90$$

$$s = (PI * r * t) / 2$$

$$x_c = 0.75 * cos(ang)$$

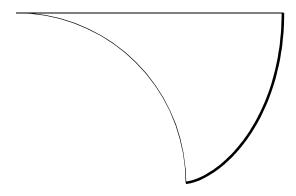
$$y_c = 0.75 * sin(ang)$$

$$x = x_c + (s * sin(ang))$$

$$y = y_c - (s * cos(ang))$$

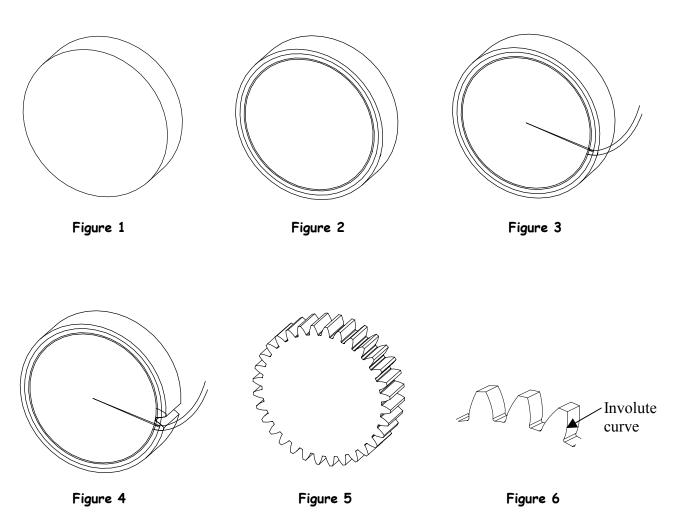
$$z = 0$$

The resulting datum curve is shown in bold below.



Creating the Gear

In Pro/ENGINEER, the gear is started by modeling a cylinder at the outside diameter of the gear, see Figure 1. Several sketches are created to define the root diameter, base diameter, and pitch diameter of the gear, see Figure 2. Next, the involute shaped datum curve is created and moved into the correct position to define one side of one gear tooth, see Figure 3. The curve is mirrored and the gear tooth is cut into the cylinder using the edge of the involute datum curves, see Figure 4. The cut is patterned and rounds are added at the base of the gear. The completed gear is shown in Figures 5 and 6.



Gear Parameters

The following are geometric parameters in gear design:

Root Diameter Circular Pitch = π / Pitch Diameter

Outside Diameter Number of Teeth = Diametrical Pitch * Pitch Diameter

Base Diameter Pressure Angle

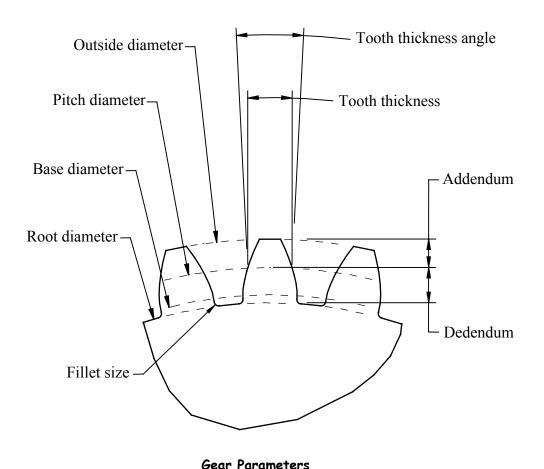
Addendum Dedendum

Tooth Thickness

Tooth Thickness Angle

Fillet Size

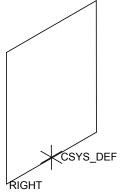
The figure describes some of the gear parameters.

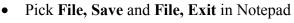


EXERCISE 4 - INVOLUTE GEARS

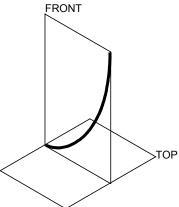
Task 1: Create a datum curve driven by an equation.

- Pick File, New, then enter < involute gear > for the name of the new part
- Pick **OK** in the **New** dialog box
- Pick Insert, Model Datum, Curve, From Equation, Done
- Select the default coordinate system, then pick Cartesian
- In the Notepad window, enter the following equations:



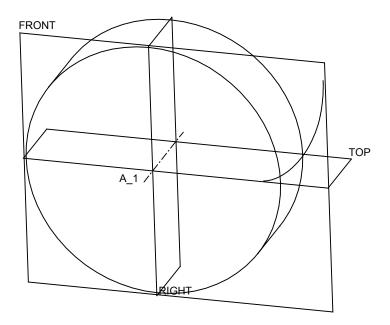


- Pick **OK** in the dialog box
- The result is shown here
- This curve will be used to create an involute gear



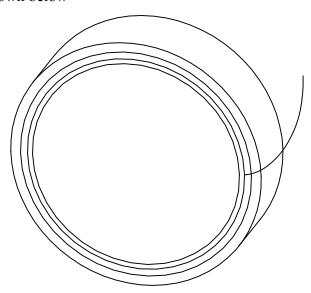
Task 2: Create a cylinder.

- Select the FRONT datum plane
- Pick the Extrude icon
- Press and hold the right mouse button and select Define Internal Sketch
- Pick Flip in the Sketch dialog box
- Pick **Sketch** in the **Sketch** dialog box
- Sketch a circle centered on the references, with a diameter of 6.500, to represent the *outside diameter* of the gear (see the figure on the previous page)
- Pick the checkmark to complete the sketch
- Enter < 1.750 > for the depth then pick the checkmark in the dashboard tool
- Pick View, Orientation, Standard Orientation
- The result is shown below, be sure the curve is in front of the cylinder as shown



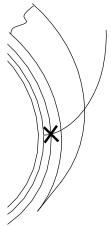
Task 3: Create three circles representing the major diameters.

- Create a circular sketch on the FRONT datum plane with a diameter of 5.376 to represent the *root diameter* of the gear
- Create a circular sketch on the FRONT datum plane with a diameter of 5.638 to represent the *base diameter* of the gear
- Create a circular sketch on the FRONT datum plane with a diameter of 6.000 to represent the *pitch diameter* of the gear
- The result is shown below



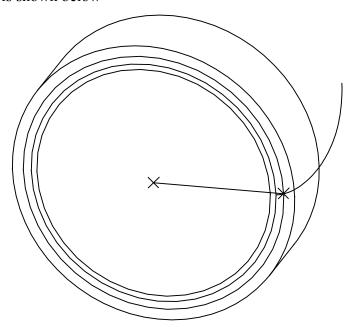
Task 4: Create a datum point.

• Set the selection filter to **Datums**, pick the involute curve **and** the 6.000 diameter circular sketch, then pick the **Point** icon and then pick **OK** to create a datum point as shown below



Task 5: Create another datum point and a datum curve.

- Be sure the selection filter is set to *Datums*
- Pick RIGHT, TOP, and FRONT then pick the Point icon $\left|\begin{array}{c} \times \\ \times \end{array}\right|$ then pick <u>OK</u>
- Pick Insert, Model Datum, Curve, Done
- Pick the two datum points then pick **Done** and **OK**
- The result is shown below

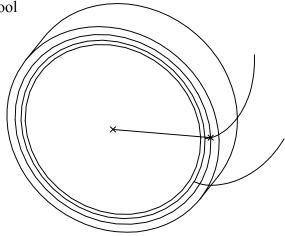


Task 6: Create a datum evaluate feature.

- Pick Insert, Model Datum, Evaluate
- Enter < measure > for the name of the feature
- Pick Create, then enter < angle > for the name of the measurement parameter
- Pick **Angle**, then pick the TOP datum plane and the curve you just created through the points
- Pick **Done** then read the message window and look at the model tree
- Save the part

Task 7: Copy the involute curve.

- Set the selection filter to *Features*
- Pick the involute curve then pick Edit, Copy
- Pick Edit, Paste Special
- Add the checkmark next to **Apply Move/Rotate transformations to copies** in the dialog box then pick **OK**
- Pick **Rotate** in the right mouse button popup menu
- Pick the axis in the center of the cylinder then enter < -30 > for the rotation angle
- Pick the checkmark in the dashboard tool
- The result is shown

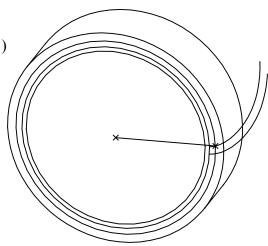


Task 8: Add a relation and regenerate the part.

- Double pick the copied involute curve (the one created in task 7)
- Double pick the 30 dimension
- In the small text box, carefully enter:

angle:FID MEASURE + (7.5/2)

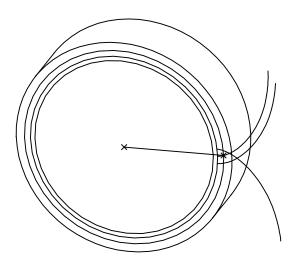
- Pick <u>Yes</u> to add the relation
- Pick Edit, Regenerate
- The result is shown



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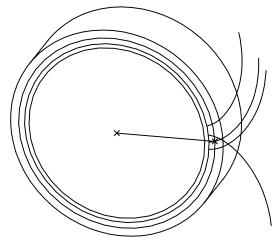
Task 9: Mirror the copied involute curve.

- Pick the copied involute curve (the one created in task 7) then pick Edit, Mirror
- Pick the TOP datum plane then pick the checkmark in the dashboard tool
- The result is shown



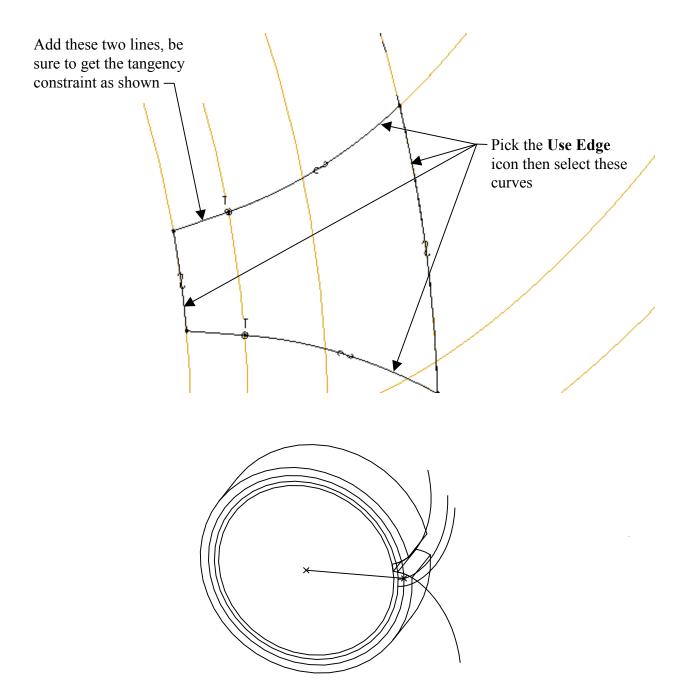
Task 10: Copy the curve again.

- Pick the copied involute curve (the one created in task 7) then pick **Edit**, **Copy**
- Pick Edit, Paste Special
- Add the checkmark next to **Apply Move/Rotate transformations to copies** in the dialog box then pick **OK**
- Pick **Rotate** in the right mouse button popup menu
- Pick the axis in the center of the cylinder then enter < -15 > for the rotation angle
- Pick the checkmark in the dashboard tool
- The result is shown



Task 11: Create an extruded cut.

- Create an extruded (through all) cut using the edges of the curves as shown below
- Trim the sketch as shown below
- The result is shown at the bottom of the page



Task 12: Pattern the cut.

- Set the selection filter to *Features* then pick the cut you just created
- Pick Edit, Pattern, then set the type of pattern to Axis in the dashboard tool
- Select the axis in the center of the cylinder
- Enter < 24 > for the number of instances in the pattern
- Enter < 15 > for the increment angle
- Pick the checkmark in the dashboard tool to complete the pattern

Task 13: Finish the part.

- Create a 0.020 round at the base of the gear tooth -
- Pattern the round
- Create a coaxial hole with a diameter of 2.000
- Use **Layers** to hide the datum curves and sketches
- The completed part is shown below
- Save the part and Close the window

